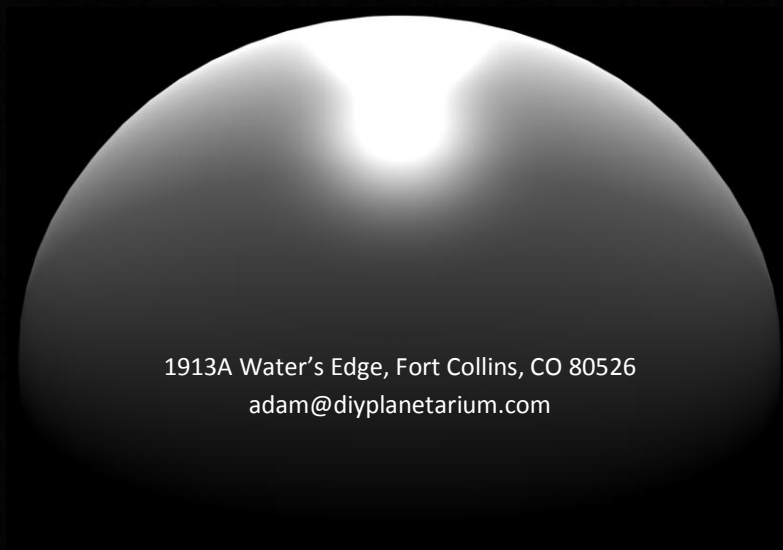


DIY PLANETARIUM



A COMPLETE DOME CONSTRUCTION GUIDE

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For more detailed terms and explanations, see the Glossary in the back of this text. The Glossary defines terms and lists the pages they appear on.



Introduction

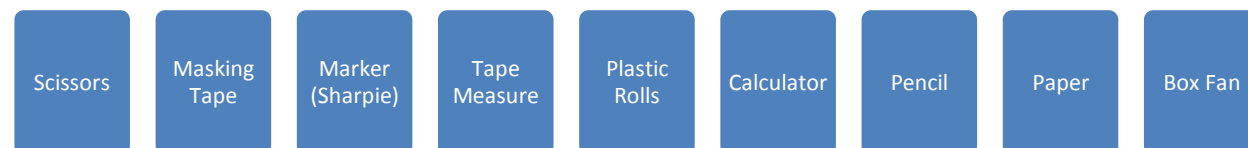
This manual is a completely new manual designed from scratch. I am qualified to write this manual as I have been building planetariums for over four years, almost have a degree in Computer Science at CSU and have studied math through Calculus II and Combinatorial Theory. This manual requires that the user knows basic trigonometry and how to manipulate trigonometric functions on a calculator. Construction methods are simple and require only that the user is very accurate when measuring dimensions and cutting out pieces.

A planetarium is a hemispherical dome constructed in a variety of geometries used to view content on a spherical surface as opposed to a flat screen. This surface adds an additional level of immersion making fulldome planetarium theaters ideal for entertainment, education and simulation. This technical manual will detail the full construction of a planetarium and its components from designing a pattern to installing digital hardware for a true fulldome projection. Great technologies tend to be *very* expensive as well. A professionally made planetarium, for example, will cost around twenty-five thousand U.S. dollars. This manual will detail all the necessary steps to produce a dome of professional quality for a budge less than twenty-five *hundred* dollars, or ten percent of that of the same manufactured product.

Materials

To construct a planetarium dome, two fields of materials will be needed. The first section is dome materials, the second, dome technology. Domes can be built out of many materials such as plastic, aluminum, cardboard and even fabric. This manual documents plastic dome construction, however, a skilled craftsman could build a dome out of any pliable material using the dimensions in this manual. Materials needed are as follows:

Dome Materials



Additional notes: Masking tape 1.5" wide works the best for taping together gore sections. Any type of plastic may be used that has a width less than two meters and can be unrolled. Dual sided plastic that is black on one side, white on the other, is the optimal choice of plastic as it



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has decent contrast for projection inside but primarily, great protection from light on the outside. This is beneficial for showing films in rooms that can't be made completely dark such as a gym as the intimate theater atmosphere is ruined with any light. White plastic will also work if double sided plastic is too expensive or unavailable. The length of plastic required for a dome of any size can be calculated using the length calculation in the *Math* section of this manual.

Dome Technology

Safety
Mirror (18")

Computer
(1080p
Capable)

Loud 2.1+
Stereo

1080p
Projector

Power
Cables

Blender
Software
(Free)

Black
Blankets
(Optional
for Floor)

The best mirror to use in a planetarium is a primary surface mirror. These mirrors are optimal because they don't have any protection on the reflection surface and thus produce the best image, however, can easily exceed several thousand dollars in price. A cheaper safety mirror can be purchased (half-hemisphere) for approximately thirty-eight dollars.

Any 1080p projector will work in a dome, especially when a budget won't permit a higher end one. A current manufacturing trend shows that more expensive projectors have both higher contrast ratios and lumen counts, ideal for the best picture quality.

Anytime a dome is inflated, it is secured to the ground. As floors can be dirty and uncomfortable, black blankets provide a clean and relaxing way to view a show without decreasing the contrast ratio. Conversely, white blankets are a poor choice for floor coverage as they both show dirt easily and reflect projected light in the dome onto the rotunda.

Math

The math portion of this manual is the heart and soul of the dome construction process. The following information is needed to calculate the planetarium blueprints:

Dome Diameter

Width of Plastic

Lateral Divisions¹

The following equations will *generate* the planetarium blueprints based on the input parameters: dome diameter, width of plastic and the number of lateral divisions. It is important to note that numbers must be in the form of the

1. The number of lateral divisions should be by default, at least 20. Increasing this number will increase the accuracy of the dome's shape.



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same unit. Numbers generated by formulas will be of this same unit. For example, if the chosen diameter is five meters, the width of the plastic needs to be listed in meters too.

Formula 1 | Number of Gore Sections Needed:

$$\text{number of sections} = \text{ceil}\left(\frac{\pi \cdot \text{diameter}}{\text{width of plastic}}\right)$$

Note: ceil(x) means to round x up to the nearest whole integer.

Formula 2 | Total Length of Plastic Needed

$$\text{length} = \frac{\frac{4}{3} \cdot \pi \cdot \left(\frac{\text{diameter}}{2}\right)^3}{4} \cdot \text{number of sections}$$

Note: the length as calculated in this function is also the total length of plastic needed to build a dome of the specified diameter.

Formula 3 | Calculating the Gore Sections

This formula is the most difficult. It will produce a *triangular* shaped section called a **gore**. As many gores as determined by the value *number of sections* needs to be made for the dome. A mathematical principle relating dome size to the number of sections shows that the number of gores required increases as does the size of the dome. The following calculations and steps will produce a gore pattern:

Formula 4 | Calculating the Gore Sections

$$\text{angle}(x) = \frac{90 \cdot x}{\text{lateral divisions}}$$

*Use the following equation to fill in the chart below. **Make sure to calculate in degrees, not radians. If your calculator does not display Degrees or Deg in its settings, pressing the Mode button on most models will cycle through modes until the calculator is operating in Degrees.***

$$\text{width at height}(x) = \frac{\cos^{-1}(x) \cdot \frac{\text{diameter}}{2} \cdot \pi \cdot 2}{\text{number of sections}}$$

Table A

Formula 3	Formula 4	Value
$\text{angle}(0) = a_0$	$\text{width at height}(a_0)$	<i>circumference/nos</i>
$\text{angle}(1) = a_1$	$\text{width at height}(a_1)$	<i>smaller</i>
...	...	...
$\text{angle}(\text{number of sections} = a_n)$	$\text{width at height}(a_n)$	0



Formula 5 | Calculating the Gore Sections

$$\text{height}(x) = \frac{\text{length} \cdot x}{\text{lateral divisions}}$$

Formula 5 needs to be incorporated into *Table A* to build complete blueprints for a gore section. This modified table would look as follows, using the values computed in *Table A*.

Table A1

Width(x)	Height(x)
width at height(a_0) ...	height(x_0) ...
width at height(a_n)	height(x_n)

Using tape as a marker on the ground, make a straight line a meter longer than the width of your plastic. Lay down a second piece of tape perpendicular to the first one meter longer than the length, positioned in the center of the first strip. Using a tape measure, mark along the second piece (strip b) the height(x) values as they occur in *Table A1*. At each height marker, lay a piece of tape corresponding to its table values' width (centered). The created pattern should now look like the picture on the right.



Once this pattern has been created, the dome will come together quickly. Place some tape along the contour of the outer tape fingers to give the gore section a clear edge. A different color can be helpful as an edge.



Roll the plastic over the pattern on the ground and trim the excess using scissors slightly open. This technique slices easily through the plastic. Books work well to hold the plastic in place. Cut as many gores as calculated in the number of sections formula.



The next step is trickiest: taping the sections together. An optional method to cutting each gore to the tip is to stop one section before the width reaches zero and make a circle to fill the



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top with a radius equal to the width closest to zero times the number of sections. Holding two sections together on a table, tape them in small pieces to ensure the curvature is taped along evenly. It helps to have a partner for this step.



Taping the top circle.



Inflating the dome, notice bottom of dome is taped down.

Tape in the filler circle last if the whole-top method was chosen.

Using remaining plastic, create a tube around the box fan at least ten feet long. Cut a hole in one gore section and mount the fan chute through this hole using tape. This hole will allow the dome to be inflated. Tape the dome to the floor and turn on the fan; the dome will inflate. Lift a flap of tape to crawl under the planetarium to enter it. To “close the door,” an operator outside the dome must reattach the tape to the floor.

In the photo below, the fan inflation unit is located on the left. Its length reduces noise inside.





Dome Technology

Compared to a conventional movie screen, planetariums vary in one fundamental way: their content is projected onto a hemisphere instead of a flat screen, often utilizing 5 or 6 projectors in a fulldome theater. This requires a special projection method called a fisheye render. Planetarium projectors utilizing fisheye projection are very expensive yet produce good results. An example of a fisheye projection is presented at right.

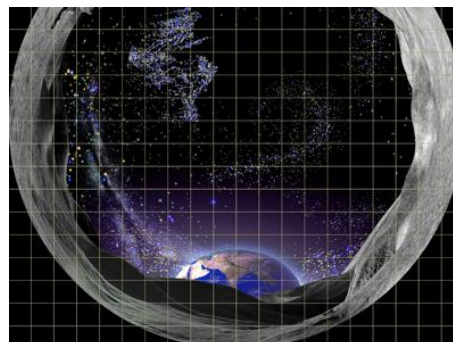
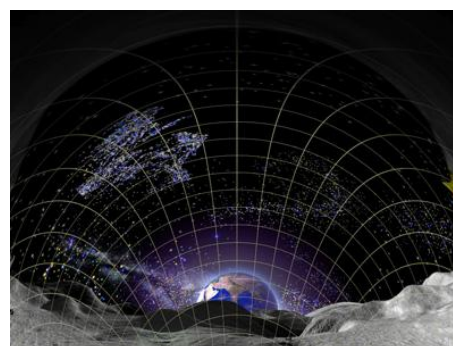


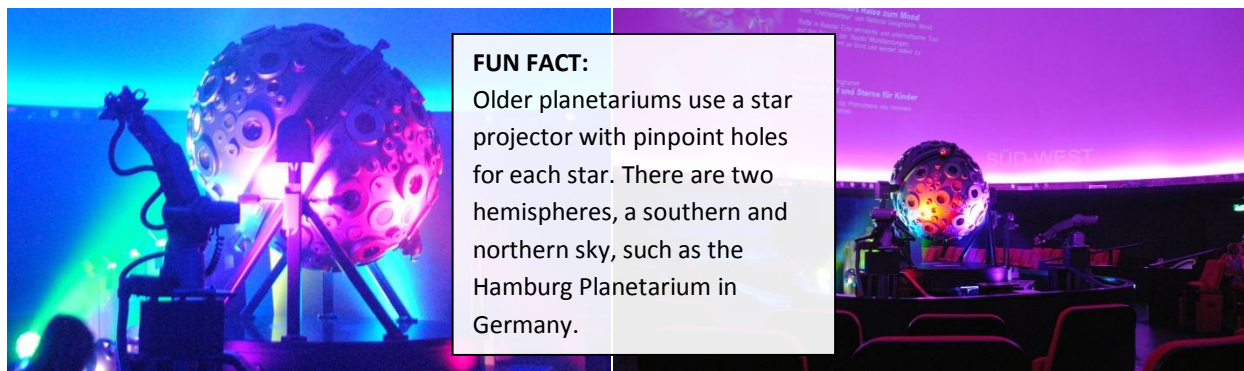
Image Credit: Paul Bourke (both images)

A cheaper alternative to this projection technology is a truncated fisheye projection used to project onto a hemisphere using a mirror dome. The resulting image can be projected with decent 1080p resolution using a single cheap projector. An example of a distorted fisheye can be seen below the original. By changing merely the *projection method*, the cost is reduced by over fourteen thousand dollars or a 15x reduction.



A single table can house all of the planetarium electronics. Point a table (3'x6') towards middle of the room. Against the dome, position the mirror with the curvature touching that of the domes. Shine the projector at the mirror and connect the laptop input. Load a file such as the truncated image on the bottom of page seven to keystone the projector and mirror.

Audio speakers should be positioned on the “opposite” side of the mirror facing the table. Blankets can be laid around the floor to help protect cables underneath, keep viewers clean and provide a comfortable atmosphere.



FUN FACT:

Older planetariums use a star projector with pinpoint holes for each star. There are two hemispheres, a southern and northern sky, such as the Hamburg Planetarium in Germany.

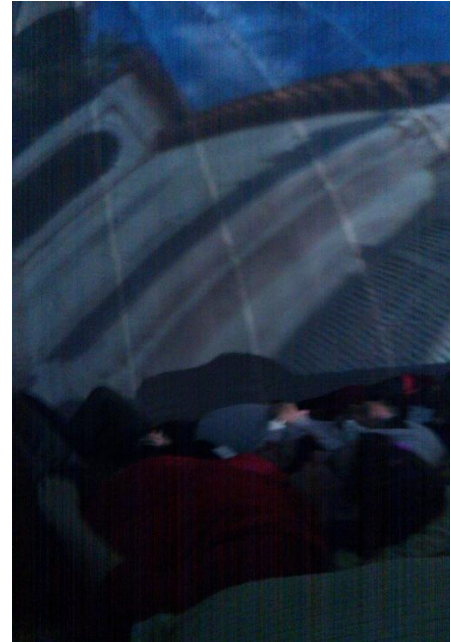


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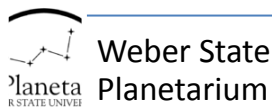
Examples of a standard setup can be seen pictured below:



The above image shows a typical mirror, projector, computer setup. The right image shows viewers inside.



Many shows are *extremely expensive*, with some annual licenses costing well over twenty thousand dollars. An alternative to purchasing shows is to create content manually using a program called Blender. For planetariums with a budget, below is a list of industry leaders in affordable pricing and quality programming:



Loch Ness
Productions



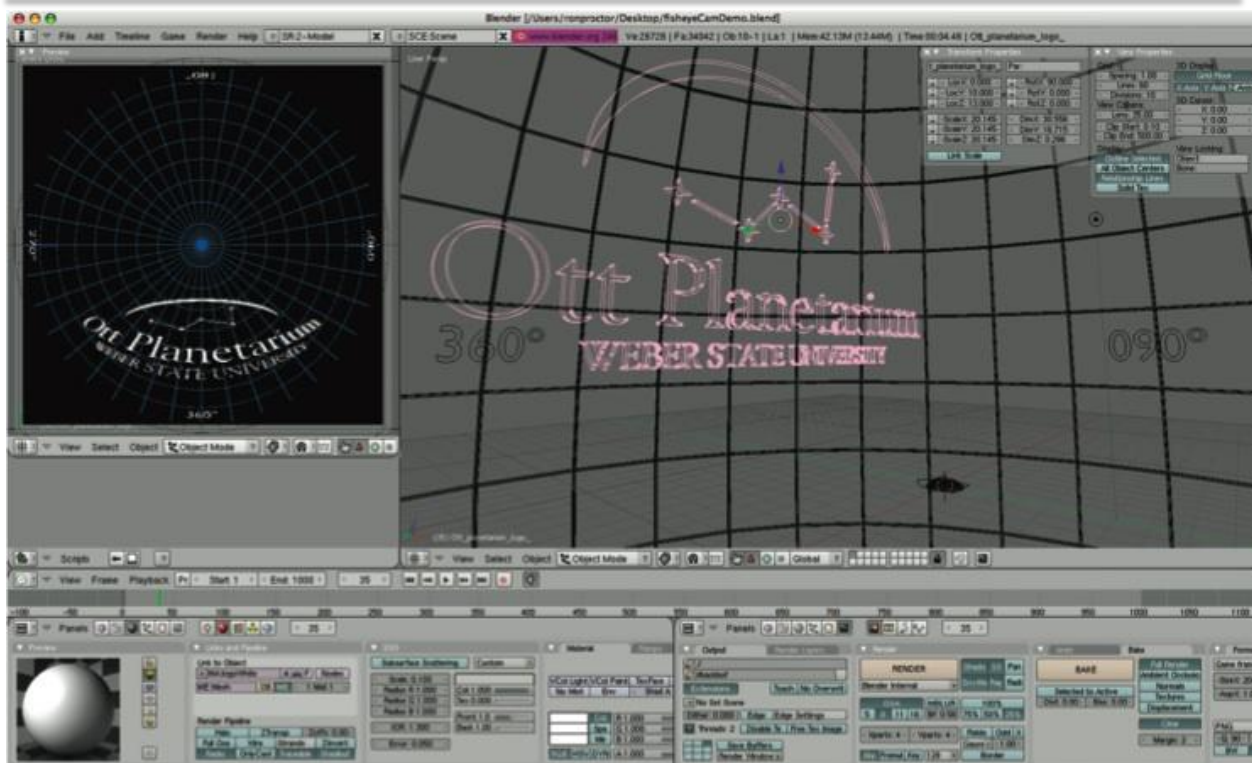
Denver Museum of
Nature & Science

Rendering Technologies

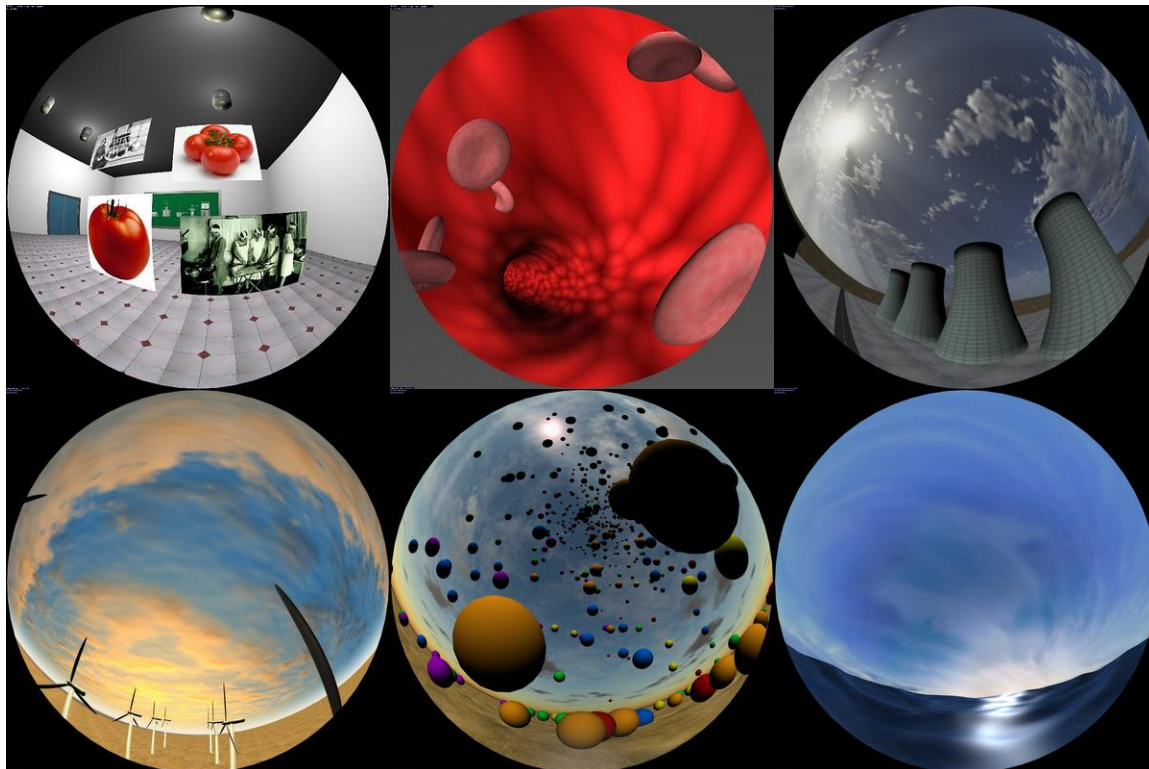
As mentioned earlier, the projection method for a planetarium is the use of a fisheye image. Render clients such as Maya and Studio 3DS Max have fisheye 'cameras' but these programs cost thousands of dollars, many with an annual license fee. Blender is a free open source alternative that provides fisheye rendering thanks to a rig developed by Ron Proctor at Weber State University. This camera rig is available upon request from the Weber State University Ott Planetarium. An image of their rig optimized bench can be found on the next page.



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Blender is an extremely powerful yet complex tool to learn. Its functionality cannot be shown documented in this manual, but the Blender Foundation sponsors hours of free lectures and tutorials available on www.blender.org. Below are some images I have rendered in Blender.





Glossary

1080p

Dome Technology

- Standard HD resolution. (1920 pixels x 1080 pixels).

Ceil

Math

- A function that rounds a number up to its nearest integer value.

Contrast Ratio

Dome Technology

- A property of a display system, defined as the ratio of the luminance of the brightest color (white) to that of the darkest color (black) that the system is capable of producing.

Gore

Math

- A bulging triangular shape that comprises a "side" of the planetarium

Half-Hemisphere

Math

- A hemisphere in halves, think of a quarter of an orange or an apple.

Hemisphere

Math

- Half of a sphere.

Lumens

Dome Technology

- The brightness of a projector.

Keystone

Dome Technology

- A process in which an image is tilted or distorted to achieve a perfect orientation.

Primary Surface Mirror

Math

- A type of mirror that has no coating on its reflective surface, making it great for optical precision, bad for durability.

Rotunda

Math

- The dome of a fixture.

Works Cited

All images in this manual are photographed by me, Adam Goss. All digital images and renderings have been rendered by me in Blender. The exceptions are the fisheye/mirrordome maps on page eight, created by Paul Bourke of Swinburne University in Australia. These images were taken from his website, www.paulbourke.net. All other content including the math is my own original work, illustrated through pictures of created content showing its efficacy.